

# Patterns of Gauge Mediation in Metastable SUSY Breaking

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Steven A. Abel<sup>a</sup>, Callum Durnford<sup>a</sup>, Joerg Jaeckel<sup>a,b</sup> and Valentin V. Khoze<sup>a</sup>

<sup>a</sup>*Institute for Particle Physics Phenomenology, University of Durham, Durham, DH1 3LE, UK*

<sup>b</sup>*Institute for Theoretical Physics, Heidelberg University,*

*Philosophenweg 16, D-69120, Heidelberg, Germany*

s.a.abel@durham.ac.uk, callum.durnford@durham.ac.uk, joerg.jaeckel@durham.ac.uk,  
valya.khoze@durham.ac.uk

**ABSTRACT:** Supersymmetry breaking in a metastable vacuum allows one to build simple and concrete models of gauge mediation. Generation of gaugino masses requires that  $R$ -symmetry be broken in this vacuum. In general, there are two possible ways to break  $R$ -symmetry, explicitly or spontaneously. We find that the MSSM phenomenology depends crucially on how this breaking occurs in the Hidden Sector. Explicit  $R$ -symmetry breaking models can lead to fairly standard gauge mediation, but we argue that in the context of ISS-type models this only makes sense if  $B = 0$  at the mediation scale, which leads to high  $\tan\beta$ . If on the other hand,  $R$ -symmetry is broken spontaneously, then  $R$ -symmetry violating soft terms tend to be suppressed with respect to  $R$ -symmetry preserving ones, and one is led to a scenario with large scalar masses. These models interpolate between standard gauge mediation and split SUSY models. We provide benchmark points for the two scenarios. They demonstrate that the specific dynamics of the Hidden Sector – the underlying nature of supersymmetry and  $R$ -symmetry breaking – affects considerably the mass spectrum of the MSSM, and vice versa.

## 1. Introduction

Supersymmetry continues to be the most compelling candidate for the theoretical framework describing particle physics beyond the Standard Model. In the current paradigm, SUSY is dynamically broken in the Hidden Sector of the full theory and the effects of this SUSY-breaking are mediated to the Visible Sector (MSSM) by so-called messenger fields. In the usual formulation, one essentially ignores the Hidden Sector theory and subsumes its details into a few parameters; the scale  $M_{SUSY}$  at which SUSY is broken in the Hidden Sector, the nature of mediation (gravity, gauge, extra dimensions, etc.) and the types of messenger fields. Thus it is tempting to assume that the details of the Hidden Sector are largely irrelevant to Visible Sector phenomenology, and that the entire pattern of the SUSY-breaking soft terms in the MSSM is generated and determined by the messengers. The recent breakthrough made by Intriligator, Seiberg and Shih (ISS) [1] in realising the dynamical SUSY breaking (DSB) via metastable vacua, provides a very minimal and simple class of candidates for the Hidden sector, and makes it natural to reexamine this assumption. In particular, is it possible to distinguish different types of Hidden Sector physics for a given type of mediation and messenger?

We shall address this question in the context of models of low scale i.e. gauge mediation (GMSB). These were introduced in the early days of SUSY model building in Refs. [2–7] and were subsequently revived in [8–10] (see [11] for a comprehensive review of GMSB patterns and phenomenology). The main advantage of gauge mediation from a phenomenological point of view is the automatic disposal of the flavour problem which plagues gravity mediation. In GMSB the messenger fields interact only with the gauge field supermultiplets in the MSSM and the gauge interactions do not generate unwanted flavour changing soft terms in the MSSM. The sfermion soft masses are universal in flavour space and the only source of flavour violation is through the Yukawa matrices, which is already incorporated correctly into the Standard Model. Furthermore, the SUSY scale in GMSB is relatively low,  $M_{SUSY} \ll \sqrt{m_W M_{Pl}}$ , and one can determine the full field theory in its entirety without appealing to the uncalculable details of an underlying supergravity theory, as one has to in gravity mediation. Indeed, the recent realisation [1] that the dynamical breaking of supersymmetry can be achieved easily in ordinary SQCD-like gauge theories implies that now one can formulate complete and calculable models of gauge mediated SUSY-breaking including the Hidden (and Visible) sectors. The goal of this paper is to study and classify these models, and to show how the generic patterns of SUSY breaking generated in the MSSM depend on the details of the Hidden Sector.

To anticipate our findings, Visible Sector phenomenology depends essentially on how  $R$ -symmetry is broken in the Hidden Sector. Explicit  $R$ -symmetry breaking models of Refs. [12, 13] can lead to fairly standard gauge mediation, but we argue that in the context of ISS-type models this only makes sense if  $B = 0$  at the mediation scale, which leads to high  $\tan\beta$ . If, on the other hand,  $R$ -symmetry is broken spontaneously, as in the model of Ref. [14], then  $R$ -symmetry violating operators in the MSSM sector (e.g. gaugino masses) tend to be suppressed with respect to  $R$ -symmetry preserving ones (e.g. scalar masses), and one is led to a scenario with large scalar masses (and of course more fine-tuning).<sup>1</sup> In the limit of small  $R$ -symmetry breaking we recover so-called split SUSY models [16, 17]. We provide

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<sup>1</sup>This kind of spectrum indicates a residual approximate  $R$ -symmetry in the model as the main cause for the sup-

benchmark points for the two scenarios as an illustration.

### 1.1 On the unavailability of metastability and on $R$ -symmetry breaking

If SUSY is discovered at the LHC and is of the gauge mediation type, then metastability of the vacuum is likely to be unavoidable [18] because of two pieces of evidence: gauginos are massive, and so too are  $R$ -axions. We will briefly discuss why this is so, in full generality and independently of the models of ISS. To see that metastability follows from these two pieces of evidence, the first important observation is the theorem by Nelson and Seiberg [19], that an exact  $R$ -symmetry is *necessary and sufficient* to break SUSY in a generic calculable theory (of the Hidden sector). At the same time, Majorana masses of gauginos have non-vanishing  $R$ -charges. Thus we have a phenomenological problem which could be called the *gaugino mass problem*: gaugino masses require both supersymmetry and  $R$ -symmetry breaking, but Ref. [19] tells us that these two requirements are mutually exclusive. How to get around it?

One approach [18] is to assume that the Lagrangian is of the form

$$\mathcal{L} = \mathcal{L}_R + \varepsilon \mathcal{L}_{R\text{-breaking}}, \quad (1.1)$$

where  $\mathcal{L}_R$  preserves  $R$ -symmetry, the second term,  $\mathcal{L}_{R\text{-breaking}}$ , is higher order in fields and breaks  $R$ -symmetry, and  $\varepsilon$  is parametrically small (we discuss why this should be shortly). Because  $R$ -symmetry is broken explicitly by the second term, the Nelson-Seiberg theorem requires that a global supersymmetry-preserving minimum must appear at order  $1/\varepsilon$  away from the SUSY breaking one which now becomes metastable. Note that this statement is completely general. Any attempt to mediate SUSY breaking to gauginos even from models that initially have no SUSY-preserving vacuum results in the appearance of a global SUSY minimum. Also the gaugino masses depend, as one would expect, on both the scale of SUSY breaking *and* the scale of  $R$ -symmetry breaking, whereas the scalar masses depend only on the former. (This point was used previously in [17] in support of split SUSY [16]). The gaugino masses are directly related to  $\varepsilon$  and hence to the stability of the metastable vacuum.

The second possibility is to break the tree-level  $R$ -symmetry spontaneously. Spontaneous (rather than explicit) breaking of  $R$ -symmetry does not introduce new global SUSY preserving minima. As such it does not destabilize the SUSY breaking vacuum and does not require any fine-tuning of coefficients in the Lagrangian. At the same time, gauginos do acquire masses. This scenario, however, leads to a massless Goldstone mode of the spontaneously broken  $U(1)_R$  symmetry – an  *$R$ -axion problem*. In order to avoid astrophysical (and experimental) bounds, the  $R$ -axion should also acquire a mass. This means that  $R$ -symmetry must also be explicitly broken and by the earlier arguments this again means that the vacuum is metastable. However in this case [14] the gaugino mass is divorced from the size of *explicit*  $R$ -breaking  $\varepsilon$  which now determines the  $R$ -axion mass instead. This

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pression of gaugino masses relative to scalars. The precise reason for this suppression (investigated in a subsequent paper [15]) is a little more complicated and is linked to the *direct* nature of gauge mediation.

exhausts the logical possibilities and shows that, for a theory with a generic superpotential where the Nelson-Seiberg theorem applies, massive gauginos and massive  $R$ -axions imply metastability.

At this point the question arises as how to generate a Lagrangian of the form (1.1). Unless there is a compelling reason for the smallness of  $\varepsilon$ , the Lagrangian  $\mathcal{L}_R$  is by definition non-generic, and  $\mathcal{L}_{R\text{-breaking}}$  may allow many couplings which are compatible with the symmetries that one has to set to be small in order to avoid too rapid decay of the metastable vacuum. One requires an *almost* non-generic model, broken by small operators, which in general seems unlikely. However, realistic and natural gauge mediation models of this type were constructed in [12, 13]. The main idea of these models is to break  $R$ -symmetry by operators which are suppressed by powers of  $M_{Pl}$ . We will consider these models in Section 3.

In [14] we suggested an alternative approach where  $\varepsilon$  is not induced by external  $1/M_{Pl}$  corrections and where  $R$ -symmetry is broken spontaneously. In the original ISS model [1], the Nelson-Seiberg theorem manifests itself in a simple way: the theory has an exact  $R$ -symmetry at tree-level. However the  $R$ -symmetry is anomalous and terms of the type  $\varepsilon \mathcal{L}_{R\text{-breaking}}$  are generated dynamically [1] without having to appeal to Planck suppressed operators. Here  $\varepsilon$  is a naturally small parameter since it is generated non-perturbatively via instanton-like configurations, which are naturally suppressed by the usual instanton factor  $e^{-8\pi^2/g^2} \ll 1$ . Hence, the non-genericity in these models is fully calculable and under control. When, in addition to these non-perturbative effects, the  $R$ -symmetry is also broken spontaneously by perturbative contributions, gauginos receive sufficiently large masses  $m_{\text{gaugino}} > 100$  GeV as required by their non-observation by current experiments. At the same time the  $R$ -axion receives a mass from the anomalously induced  $R$ -breaking terms. (Note that a possible additional contribution to the  $R$ -axion mass may arise when the theory is embedded in supergravity [20]. However such noncalculable effects are suppressed.)

The spontaneous breaking of  $R$ -symmetry by radiative perturbative corrections is easy to achieve [21, 22]. For example, this happens [14] when the basic ISS model is deformed by adding a baryon-like term to the superpotential. This is the simplest deformation of the ISS model which preserves  $R$ -symmetry at tree-level. At one-loop level this deformation causes the  $R$ -symmetry to break spontaneously, while the  $R$ -axion gets a sufficiently large mass  $m_{\text{axion}} > 100$  MeV to avoid astrophysical constraints from the non-perturbative anomalous  $R$ -symmetry breaking [14]. No new global minima appear other than those of the original ISS model, so the SUSY breaking scale can be sufficiently low to be addressed at the LHC. These models will be discussed in Section 2.

The paper is organised as follows. For convenience, in the following Section we recall the original ISS model [1]. In Section 2 we study gauge mediation with spontaneous  $R$ -symmetry breaking. Specifically, we concentrate on the *direct* gauge mediation model [14] where the Hidden plus Messenger sectors consist of only the baryon-deformed ISS theory with  $N_f = 7$  flavours and  $N_c = 5$  colours. The resulting gaugino and sfermion soft masses are discussed in Section 2.2. The mass term for the  $R$ -axion is generated by the nonperturbative ISS superpotential (1.3), as explained in [14]. In Section 2.3 we analyse the phenomenology of this class of models, which turns out to be quite different from the usual gauge mediation scenarios [11]. The main reason for this difference is the fact that  $R$ -symmetry is

broken spontaneously by one-loop corrections, and as such the scale of  $R$ -breaking is naturally smaller than the scale of SUSY-breaking, leading to the gaugino masses being smaller than the scalar masses. This is different from the usual gauge-mediation assumption that the  $R$ -symmetry breaking is larger than the SUSY breaking. Thus generally, one expects a Hidden sector with spontaneous  $R$ -symmetry violation to interpolate between standard gauge mediation and split SUSY models [16, 17].

In Section 3 we study the alternative scenario for metastable gauge mediation, formulated earlier in Refs. [12, 13]. These are models with an explicit messenger sector where the  $R$ -symmetry of the ISS sector here is broken explicitly. As already mentioned, the reason why the effective  $R$ -symmetry breaking is weak in this case is the fact that the messengers are coupled to the Hidden Sector fields only via  $1/M_{Pl}$ -suppressed operators, cf. (3.1). In the limit where  $M_{Pl} \rightarrow \infty$ , both the  $R$ -symmetry and supersymmetry of the MSSM are exact, since the ISS Hidden Sector decouples from the messengers. As a result, in these models the effective  $R$ -symmetry breaking and the effective SUSY-breaking scales in the Visible Sector are essentially the same. The generated gaugino and scalar soft mass terms are of the same order, and the resulting phenomenology of models [12, 13] is largely of the usual form.

In both cases we will be treating the  $\mu_{\text{MSSM}}$  parameter of the MSSM as a free parameter. As it is SUSY preserving it does not have to be determined by the ISS Hidden Sector, and we will for this discussion have little to say about it: we will not address the question of why it should be of order the weak scale, the so-called  $\mu$  problem. However the corresponding SUSY breaking parameter,  $B$  or more precisely  $B\mu_{\text{MSSM}}$ , cannot consistently be taken to be a free parameter. It is determined by the models at the messenger scale, and in both cases it is approximately zero, as will be explained in detail.

## 1.2 The ISS model – summary

In Ref. [1] Intriligator, Seiberg and Shih pointed out that metastable SUSY-breaking vacua can arise naturally and dynamically in low-energy limits of supersymmetric gauge theories. The simplest prototype model is SQCD with the gauge group  $SU(N_c)$  and  $N_f$  pairs of (anti)-fundamental quark supermultiplets  $Q, \tilde{Q}$ . Metastable vacua  $|\text{vac}\rangle_+$  occur in this model when  $N_f$  is in the ‘free magnetic range’,  $N_c + 1 \leq N_f \leq \frac{3}{2}N_c$ . These vacua are apparent in the Seiberg dual formulation of the theory, which has the advantage of being weakly coupled in the vicinity of  $|\text{vac}\rangle_+$ . The magnetic Seiberg dual of the ISS theory is given [23, 24] by the  $SU(N)_{mg}$  gauge theory, where  $N = N_f - N_c$ , coupled to  $N_f$  magnetic quark/anti-quark pairs  $\varphi, \tilde{\varphi}$ . The tree-level superpotential of the magnetic theory is of the form,

$$W_{\text{cl}} = \Phi_{ij} \varphi_i \cdot \tilde{\varphi}_j - \mu_{ij}^2 \Phi_{ji} \quad (1.2)$$

where  $i, j = 1 \dots N_f$  are flavour indices and  $\Phi_{ij}$  is the gauge-singlet meson superfield, which is related to the original electric quarks via  $\Phi_{ij} \propto \Lambda^{-1} Q_i \cdot \tilde{Q}_j$  and  $\Lambda$  is the dynamical scale of the ISS theory [1]. The matrix  $\mu_{ij}^2$  (which can be diagonalised without loss of generality) arises from the masses of electric quarks,  $\mu_{ii}^2 = \Lambda m_{Q_i}$ , and is taken to be much smaller than the UV cutoff of the magnetic theory,  $\mu \ll \Lambda$ . This magnetic theory is free and calculable in the IR and becomes strongly coupled in the

UV where one should use instead the electric Seiberg dual, i.e. the original  $SU(N_c)$  SQCD which is asymptotically free.

The usual holomorphicity arguments imply that the superpotential (1.2) receives no corrections in perturbation theory. However, there is a non-perturbative contribution to the full superpotential of the theory,  $W = W_{\text{cl}} + W_{\text{dyn}}$ , which is generated dynamically [1] and is given by

$$W_{\text{dyn}} = N \left( \frac{\det_{N_f} \Phi}{\Lambda^{N_f - 3N}} \right)^{\frac{1}{N}} \quad (1.3)$$

The authors of [1] have studied the vacuum structure of the theory and established the existence of the metastable vacuum  $|\text{vac}\rangle_+$  with non-vanishing vacuum energy  $V_+$  as well as the (set of  $N_c$ ) SUSY preserving stable vacua  $|\text{vac}\rangle_0$ .

This supersymmetry breaking vacuum  $|\text{vac}\rangle_+$  originates from the so-called rank condition, which implies that there are no solutions to the F-flatness equation<sup>2</sup>

$$F_{\Phi_{ij}} = (\varphi_i \cdot \tilde{\varphi}_j - \mu_{ij}^2) = 0 \quad (1.4)$$

for the classical superpotential  $W_{\text{cl}}$ . The SUSY preserving vacua (1.6) appear by allowing the meson  $\Phi$  to develop a VEV which is stabilised by the non-perturbative superpotential (1.3) and can be interpreted in the ISS model as a non-perturbative or dynamical restoration of supersymmetry [1]. The lowest lying SUSY-breaking vacuum  $|\text{vac}\rangle_+$  is characterised by

$$\langle \varphi \rangle = \langle \tilde{\varphi}^T \rangle = \begin{pmatrix} \text{diag}(\mu_1, \dots, \mu_N) \\ 0_{N_f - N} \end{pmatrix}, \quad \langle \Phi \rangle = 0, \quad V_+ = \sum_{i=N+1}^{N_f} |\mu_i^4|. \quad (1.5)$$

Here  $\mu_i$  are the ordered eigenvalues  $\mu$  matrix, such that  $|\mu_1| \geq |\mu_2| \geq \dots \geq |\mu_{N_f}|$ . In this way, the vacuum energy  $V_+$  above receives contributions from  $(N_f - N)$  of the smallest  $\mu$ 's while the VEV  $\langle \varphi \rangle$  is determined by the largest  $\mu$ 's.

The SUSY-preserving vacuum  $|\text{vac}\rangle_0$  is described by<sup>3</sup>

$$\langle \varphi \rangle = \langle \tilde{\varphi}^T \rangle = 0, \quad \langle \Phi \rangle = \left( \frac{\Lambda}{\mu} \right)^{\frac{N_f - N}{N_f - 3N}} \mu \mathbb{1}_{N_f}, \quad V_0 = 0, \quad (1.6)$$

where for simplicity we have specialised to the degenerate case,  $\mu_{ij} = \mu \delta_{ij}$ . For  $\mu/\Lambda \ll 1$  the metastable vacuum is exponentially long-lived and the lifetime of  $|\text{vac}\rangle_+$  can easily be made much longer than the age of the Universe. One very attractive feature of these models is that at high temperatures the SUSY breaking vacua are dynamically favoured over the SUSY preserving ones [25]. This is because the metastable ISS-type vacua have more light degrees of freedom, so the early Universe would naturally have been driven into them [25–28].

Other recent investigations of metastable SUSY-breaking applied to model building include Refs. [29–39]

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<sup>2</sup>Equation (1.4) can only be satisfied for a rank- $N$  submatrix of the  $N_f \times N_f$  matrix  $F_\Phi$ .

<sup>3</sup>In fact there are precisely  $N_f - N = N_c$  of such vacua differing by the phase  $e^{2\pi i/(N_f - N)}$  as required by the Witten index of the electric ISS theory.

## 2. Gauge mediation with Spontaneous $R$ -symmetry breaking

The metastable model building paradigm makes it relatively easy to construct models with dynamically broken supersymmetry. The simplicity of the resulting models now compels us to consider the attractive possibility of *direct* gauge mediation, whereby matter fields of the SUSY-breaking sector carry charges under the gauge groups of the Standard Model and there is no need for a separate messenger sector. In ordinary gauge mediation, the details of SUSY breaking are generally ‘hidden’ from the matter sector, with the most important phenomenological features arising from the messenger particle content. The elegance of direct gauge mediation models lies in their compactness and predictivity. Previously direct mediation of metastable SUSY breaking was considered in this context in Refs. [30,31] and [14].

The essential difference between the direct gauge mediation of SUSY-breaking and the models with explicit messengers [12,13] is that the ‘direct messengers’ form an integral part of the Hidden ISS sector, and as such, their interactions with the SUSY-breaking VEVs are not suppressed by inverse powers of  $M_{Pl}$ . This means that the  $R$ -symmetry of the SUSY-breaking sector (required by the existence of the SUSY-breaking vacuum) cannot be an accidental symmetry which is violated in the full theory only by  $1/M_{Pl}$  corrections, as in [12,13]. On the other hand, any large explicit violations of  $R$ -symmetry in the full theory will necessarily destabilise the SUSY-breaking metastable vacuum. Thus, it was proposed in our earlier paper [14] that the  $R$ -symmetry must be *spontaneously* broken by radiative corrections arising from the Coleman-Weinberg potential. In this case the Nelson-Seiberg theorem does not force upon us a nearby supersymmetric vacuum and at the same time non-zero gaugino masses can be generated since the  $R$ -symmetry is broken.

We will show below that in this approach the direct gauge mediation scenarios give phenomenology quite distinct from the usual gauge mediation scenarios [11].

### 2.1 The baryon-deformed ISS model [14]

To break supersymmetry we take an ISS model with  $N_c = 5$  colours and  $N_f = 7$  flavours, which has a magnetic dual description as an  $SU(2)$  theory, also with  $N_f = 7$  flavours.<sup>4</sup> Following [14] we now deform this theory by the addition of a baryonic operator. The superpotential of the theory is given by

$$W = \Phi_{ij}\varphi_i\cdot\tilde{\varphi}_j - \mu_{ij}^2\Phi_{ji} + m\varepsilon_{ab}\varepsilon_{rs}\varphi_r^a\varphi_s^b \quad (2.1)$$

where  $i, j = 1\dots 7$  are flavour indices,  $r, s = 1, 2$  run over the first two flavours only, and  $a, b$  are  $SU(2)$  indices. This is the superpotential of ISS with the exception of the last term which is a baryon of the magnetic  $SU(2)$  gauge group. Note that the 1,2 flavour indices and the 3...7 indices have a different status and the full flavour symmetry  $SU(7)_f$  is broken explicitly to  $SU(2)_f \times SU(5)_f$ . The  $SU(5)_f$

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<sup>4</sup>These are the minimal allowed values of  $N_c$  and  $N_f$  which lead to a non-trivial – in this case  $SU(2)$  – magnetic gauge group.

	$SU(2)$	$SU(2)_f$	$SU(5)_f$	$U(1)_R$
$\Phi_{ij} \equiv \begin{pmatrix} Y & Z \\ \tilde{Z} & X \end{pmatrix}$	$\mathbf{1}$	$\begin{pmatrix} Adj + \mathbf{1} & \bar{\square} \\ \square & \mathbf{1} \end{pmatrix}$	$\begin{pmatrix} \mathbf{1} & \square \\ \bar{\square} & Adj + \mathbf{1} \end{pmatrix}$	2
$\varphi \equiv \begin{pmatrix} \phi \\ \rho \end{pmatrix}$	$\square$	$\begin{pmatrix} \bar{\square} \\ \mathbf{1} \end{pmatrix}$	$\begin{pmatrix} \mathbf{1} \\ \bar{\square} \end{pmatrix}$	1
$\tilde{\varphi} \equiv \begin{pmatrix} \tilde{\phi} \\ \tilde{\rho} \end{pmatrix}$	$\bar{\square}$	$\begin{pmatrix} \square \\ \mathbf{1} \end{pmatrix}$	$\begin{pmatrix} \mathbf{1} \\ \square \end{pmatrix}$	-1

**Table 1:** We list matter fields and their decomposition under the gauge  $SU(2)$ , the flavour  $SU(2)_f \times SU(5)_f$  symmetry, and their charges under the  $R$ -symmetry of the model in (2.1).

factor is gauged separately and identified with the parent  $SU(5)$  gauge group of the standard model. The matter field decomposition under the magnetic  $SU(2)_{gauge} \times SU(5)_f \times SU(2)_f$  and their  $U(1)_R$  charges are given in Table 1.

It is known that the  $R$ -symmetry of the ISS SQCD manifests itself only as an approximate symmetry of the magnetic formulation which is broken explicitly in the electric theory by the mass terms of electric quarks  $m_Q$ . (It is also broken anomalously, but this is already accounted for by the dynamical superpotential (1.3).) In the Appendix we point out that the  $R$ -symmetry is broken in the electric theory in a controlled way by small parameter,  $m_Q/\Lambda = \mu^2/\Lambda^2 \ll 1$ . As such the  $R$ -symmetry is preserved to that order in the superpotential.

Thanks to the baryon deformation, the model has  $R$ -charges that are not 0 or 2. As discussed in Ref. [22] this condition is necessary for Wess-Zumino models to spontaneously break  $R$ -symmetry. Therefore, our model allows for spontaneous  $R$  symmetry breaking and we have shown in [14] that this does indeed happen. We also stress that our baryon deformation is the leading order deformation of the ISS model that is allowed by  $R$ -symmetry of the full theory imposed at the Lagrangian level. As explained in the Appendix, this is a self-consistent approach since  $R$ -symmetry breaking in the electric theory is controlled by a small parameter. Terms quadratic in the meson  $\Phi$  that could arise from lower dimensional irrelevant operators in the electric theory are forbidden by  $R$ -symmetry. Thus, our deformation is described by a *generic* superpotential and (2.1) gives its leading-order terms.

Using the  $SU(2)_f \times SU(5)_f$  symmetry, the matrix  $\mu_{ij}^2$  can be brought to a diagonal form

$$\mu_{ij}^2 = \begin{pmatrix} \mu^2 \mathbf{I}_2 & 0 \\ 0 & \hat{\mu}^2 \mathbf{I}_5 \end{pmatrix}. \quad (2.2)$$

We will assume that  $\mu^2 > \hat{\mu}^2$ . The parameters  $\mu^2$ ,  $\hat{\mu}^2$  and  $m$  have an interpretation in terms of the electric theory:  $\mu^2 \sim \Lambda m_Q$  and  $\hat{\mu}^2 \sim \Lambda \hat{m}_Q$  come from the electric quark masses  $m_Q$ ,  $\hat{m}_Q$ , where  $\Lambda$  is the ISS scale. The baryon operator can be identified with a corresponding operator in the electric theory. Indeed the mapping from baryons  $B_E$  in the electric theory to baryons  $B_M$  of the magnetic



theory, is  $B_M \Lambda^{-N} \leftrightarrow B_E \Lambda^{-N_c}$  (we neglect factors of order one). Thus one expects

$$m \sim M_{Pl} \left( \frac{\Lambda}{M_{Pl}} \right)^{2N_c - N_f} = \frac{\Lambda^3}{M_{Pl}^2}, \quad (2.3)$$

where  $M_{Pl}$  represents the scale of new physics in the electric theory at which the irrelevant operator  $B_M$  is generated.

As explained in [14], this theory has a classical runaway direction  $\langle \tilde{\varphi} \rangle \rightarrow \infty$  (with  $\langle \tilde{\varphi} \rangle \langle \varphi \rangle$  fixed) to a non-supersymmetric vacuum. The quantum dynamics, namely the one-loop Coleman-Weinberg potential [40],

$$V_{\text{eff}}^{(1)} = \frac{1}{64\pi^2} \text{STr } \mathcal{M}^4 \log \frac{\mathcal{M}^2}{\Lambda_{UV}^2} \equiv \frac{1}{64\pi^2} \left( \text{Tr } m_{sc}^4 \log \frac{m_{sc}^2}{\Lambda_{UV}^2} - 2 \text{Tr } m_f^4 \log \frac{m_f^2}{\Lambda_{UV}^2} + 3 \text{Tr } m_v^4 \log \frac{m_v^2}{\Lambda_{UV}^2} \right) \quad (2.4)$$

stabilises the runaway at a point which breaks both supersymmetry and  $R$ -symmetry, thus creating a meta-stable vacuum state. ( $m_{sc}$ ,  $m_f$  and  $m_v$  on the RHS denote mass matrices of all relevant scalar, fermion and vector fields in the model and  $\Lambda_{UV}$  is traded for a renormalisation scale at which the couplings are defined.) We parameterise the classically pseudo-Goldstone and runaway VEVs by

$$\langle \tilde{\phi} \rangle = \xi \mathbf{I}_2 \quad \langle \phi \rangle = \kappa \mathbf{I}_2 \quad (2.5)$$

$$\langle Y \rangle = \eta \mathbf{I}_2 \quad \langle X \rangle = \chi \mathbf{I}_5. \quad (2.6)$$

These are the most general vevs consistent with the tree level minimization. It can be checked that at one loop order all other field vevs are zero in the lowest perturbative vacuum. By computing the masses of all fluctuations about this valley we can go about constructing the one-loop effective potential from eq. (2.4). We have done this numerically using *Vsape* program of Ref. [41]. Table 2 gives a sample points showing the VEVs stabilised by the one loop effective potential.

$\mu$	$m$	$\xi$	$\kappa$	$\eta$	$\chi$
10	0.3	41.0523	2.43592	-0.035477	-1.761261
1.1	0.3	2.1370	0.566214	-0.148546	-0.083296
1.01	0.3	1.8995	0.537043	-0.155796	-0.073474
1.003	0.3	1.8809	0.534848	-0.157752	-0.072738

**Table 2:** Stabilised VEVs from Vsape for various parameter points. All values are given in units of  $\hat{\mu}$ .

To summarise, we have identified a SUSY-breaking vacuum of the deformed ISS model, which also breaks  $R$ -symmetry spontaneously via radiative corrections. This is a long-lived metastable vacuum. The SUSY-preserving vacua of this model are only those generated by the non-perturbative superpotential,

$$W_{np} = 2\Lambda^3 \left[ \det \left( \frac{\Phi}{\Lambda} \right) \right]^{\frac{1}{2}}. \quad (2.7)$$

Adapting the supersymmetric vacuum solution from the ISS model to our case with  $\mu > \hat{\mu}$  we find,

$$\varphi = 0, \quad \tilde{\varphi} = 0, \quad \eta = \hat{\mu}^2 \mu^{-\frac{6}{5}} \Lambda^{\frac{1}{5}} \quad \chi = \mu^{\frac{4}{5}} \Lambda^{\frac{1}{5}}. \quad (2.8)$$

Note that the supersymmetric minimum lies at  $\varphi = \tilde{\varphi} = 0$  and is completely unaffected by the baryon deformation. As we are not breaking  $R$ -symmetry explicitly, no other supersymmetric vacua are generated, and, as a result, the decay rate of our metastable vacuum is exponentially small as in the original ISS model.

## 2.2 Direct gauge mediation and generation of gaugino and sfermion masses

As mentioned earlier, the  $SU(5)_f$  symmetry of the superpotential (2.1) is gauged and identified with the parent  $SU(5)$  of the MSSM sector. This induces direct gauge mediation of SUSY breaking from the metastable vacuum of the Hidden ISS sector to the MSSM. The Hidden sector matter fields  $\rho$ ,  $\tilde{\rho}$ ,  $Z$ ,  $\tilde{Z}$  and  $X$  are charged under the  $SU(5)$  and serve as direct messengers. These induce all the soft SUSY-breaking terms in the MSSM sector, including gaugino and sfermion masses.

Gaugino masses are generated at one loop order (cf. Fig. 1). The fields propagating in the loop are fermion and scalar components of the direct mediation ‘messengers’  $\rho$ ,  $\tilde{\rho}$  and  $Z$ ,  $\tilde{Z}$ .<sup>5</sup> Since gaugino masses are forbidden by  $R$ -symmetry one crucial ingredient in their generation is the presence of a non-vanishing  $R$ -symmetry breaking VEV - in our case  $\langle\chi\rangle$  generated by the non-vanishing baryon deformation  $m$ .

In contrast to the gaugino masses  $m_\lambda$ , sfermion masses  $m_{\tilde{f}}$  are not protected by  $R$ -symmetry. Hence, as long as supersymmetry remains broken, we can have non-vanishing sfermion masses even in the absence of an  $R$ -symmetry breaking VEV. In our model that means that the sfermion masses are non-vanishing even in the case of a vanishing baryon deformation. This shows that in a general (gauge) mediation scenario sfermion and gaugino masses are generated by quite different mechanisms. Accordingly the simple relation  $m_\lambda \sim m_{\tilde{f}}$  does not necessarily hold in general gauge mediation scenarios. Indeed our model is an explicit example where it fails.

Let us now turn to the practical evaluation of the gaugino masses. For fermion components of the messengers,

$$\psi = (\rho_{ia}, Z_{ir})_{ferm}, \quad \tilde{\psi} = (\tilde{\rho}_{ia}, \tilde{Z}_{ir})_{ferm}, \quad (2.9)$$

the mass matrix is given by

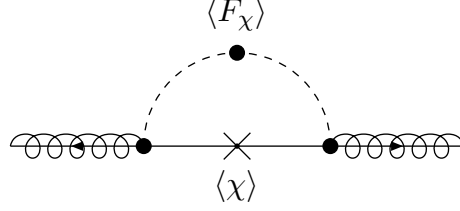
$$m_f = \mathbf{I}_5 \otimes \mathbf{I}_2 \otimes \begin{pmatrix} \chi & \xi \\ \kappa & 0 \end{pmatrix}. \quad (2.10)$$

We can also assemble the relevant scalars into

$$S = (\rho_{ia}, Z_{ir}, \tilde{\rho}_{ia}^*, \tilde{Z}_{ir}^*)_{sc}, \quad (2.11)$$

---

<sup>5</sup>The adjoint part in  $X$  is also charged under the standard model gauge groups and therefore, in principle, can also mediate SUSY-breaking. However, at tree-level  $X$  does not couple to the supersymmetry breaking  $F$ -term, and its fermionic and bosonic components have identical (zero) mass. This degeneracy is only lifted at the one-loop level by the Coleman-Weinberg potential. We therefore neglect the contribution from  $X$  which we expect to be subdominant.



**Figure 1:** One-loop contribution to the gaugino masses. The dashed (solid) line is a bosonic (fermionic) messenger. The blob on the scalar line indicates an insertion of  $\langle F_\chi \rangle$  into the propagator of the scalar messengers and the cross denotes an insertion of the  $R$ -symmetry breaking VEV into the propagator of the fermionic messengers.

and for the corresponding scalar mass-squared matrix we have

$$m_{sc}^2 = \mathbf{I}_5 \otimes \mathbf{I}_2 \otimes \begin{pmatrix} |\xi|^2 + |\chi|^2 & \chi^* \kappa & -\hat{\mu}^2 & \eta \kappa \\ \chi \kappa^* & |\kappa|^2 & \xi \eta + 2m\kappa & 0 \\ -\hat{\mu}^2 & (\xi \eta)^* + 2m\kappa^* & |\kappa|^2 + |\chi|^2 & \chi \xi^* \\ \eta^* \kappa^* & 0 & \chi^* \xi & |\xi|^2 \end{pmatrix}. \quad (2.12)$$

Gaugino masses arise from the one-loop diagram in Fig. 1. To evaluate the diagram it is convenient to diagonalize the non-diagonal mass terms (2.10), (2.12) using unitary matrices,

$$\hat{m}_{sc}^2 = Q^\dagger m_{sc}^2 Q \quad (2.13)$$

$$\hat{m}_f = U^\dagger m_f V. \quad (2.14)$$

The fields in the new basis are given by,

$$\hat{S} = S.Q \quad (2.15)$$

$$\hat{\psi}_+ = \psi.U \quad (2.16)$$

$$\hat{\psi}_- = \tilde{\psi}.V^*. \quad (2.17)$$

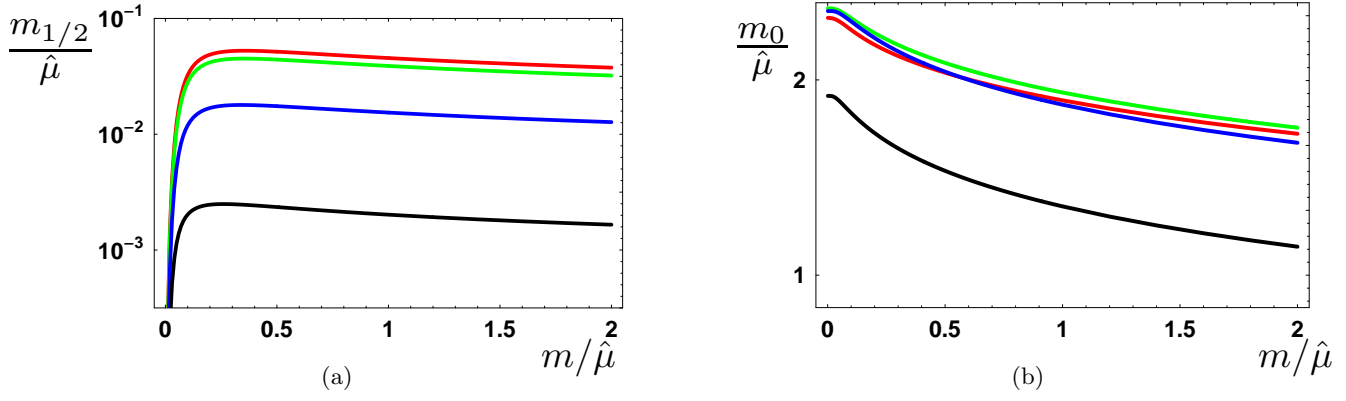
In order to calculate the gaugino mass, we need the gauge interaction terms given by

$$\mathcal{L} \supset i\sqrt{2}g_A\lambda_A(\psi_1 T^A S_1^* + \psi_2 T^A S_2^* + \tilde{\psi}_1 T^{*A} S_3 + \tilde{\psi}_2 T^{*A} S_4) + H.C. \quad (2.18)$$

$$= i\sqrt{2}g_A\lambda_A(\hat{\psi}_{+i}\hat{S}_k^*(U_{i1}^\dagger Q_{1k} + U_{i2}^\dagger Q_{2k}) + \hat{\psi}_{-i}\hat{S}_k(Q_{k3}^\dagger V_{1i} + Q_{k4}^\dagger V_{2i})) + H.C, \quad (2.19)$$

where we have expressed everything in terms of the mass eigenstates in the second line.

Using the gauge interactions Eq. (2.19), the diagram in Fig. 1 contributes to gaugino masses as



**Figure 2:** Gaugino mass scale,  $m_{1/2}$ , and sfermion mass scale,  $m_0$ , as functions of the baryon deformation  $m$ , for various values of  $\mu$ : red ( $\mu = 1.003$ ), green ( $\mu = 1.01$ ), blue ( $\mu = 1.1$ ) and black ( $\mu = 1.5$ ). The mass scales  $m_{1/2}$  and  $m_0$  are defined in Eqs. (2.27),(2.28).

follows<sup>6</sup>,

$$m_{\lambda_A} = 2g_A^2 \text{Tr}(T^A T^B) \sum_{ik} (U_{i1}^\dagger Q_{1k} + U_{i2}^\dagger Q_{2k})(Q_{k3}^\dagger V_{1i} + Q_{k4}^\dagger V_{2i}) I(\hat{m}_{f,i}, \hat{m}_{sc,k}) \quad (2.20)$$

where the 1-loop integral  $I$  evaluates to

$$I(a, b) = \frac{-a(\eta + 1)}{16\pi^2} + \frac{1}{16\pi^2} \frac{a}{a^2 - b^2} (a^2 \log(a^2/\Lambda^2) - b^2 \log(b^2/\Lambda^2)), \quad (2.21)$$

$$\eta = \frac{2}{4 - D} + \log(4\pi) - \gamma_E. \quad (2.22)$$

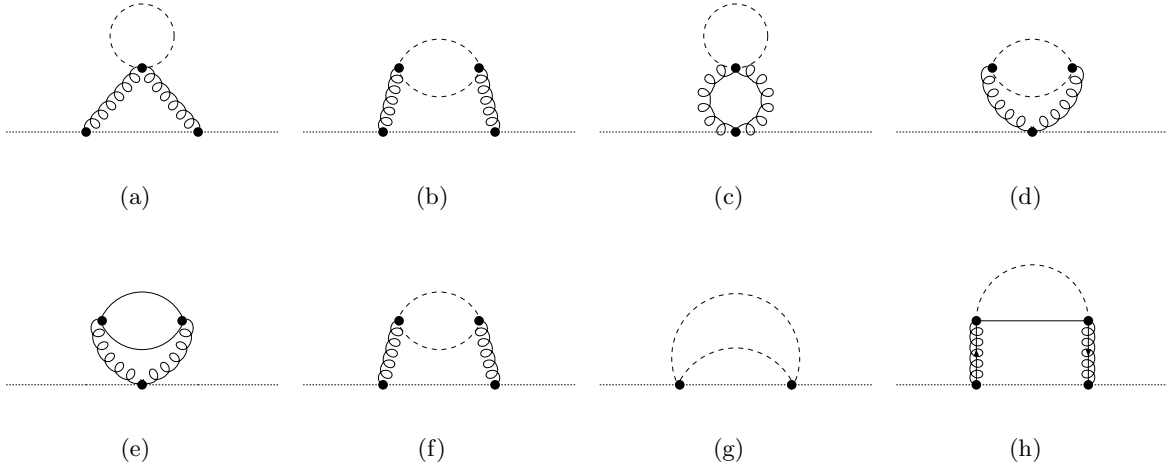
$I(a, b)$  is UV-divergent, but the divergences cancel in the sum over eigenstates as they should.

Keeping the SUSY-breaking scale  $\hat{\mu}$  fixed we can now study the dependence of the gaugino mass on the two remaining parameters  $\mu$  and  $m$ . The VEVs  $\xi$ ,  $\kappa$ ,  $\eta$  and  $\chi$  are generated from minimizing the effective potential, as above. The results are shown in Fig. 2(a).

For completeness we note that the usual analytic expression for the gaugino mass valid to the leading order  $\mathcal{O}(F_\chi)$ , is of little use for us. It comes from magnetic quarks,  $\rho$  and  $\tilde{\rho}$ , propagating in the loop, as shown in Fig. 1, and takes form  $m_{\lambda_A}^{(1)} \sim \frac{g_A^2}{16\pi^2} F_\chi (m_f)_{11}^{-1}$ . However it trivially vanishes in our model, and one needs to go to order  $F_\chi^3$  to find a non-vanishing contribution. This effect was first pointed out in Ref. [42]: the zero element in the lower right corner of the fermion mass matrix (2.10) implies that  $(m_f)_{11}^{-1} = 0$  and hence  $m_{\lambda_A}^{(1)} = 0$ .

Having determined the gaugino masses in Eq. (2.20) and Fig. 2(a), we now turn to the generation of the masses for the sfermions of the supersymmetric standard model. Here we will closely follow the calculation in Ref. [43] adapted to our more general set of messenger particles. As already mentioned at the beginning of this section, sfermion masses are generated by a different mechanism than the

<sup>6</sup>More precisely, in evaluating (2.20), we use the diagram in Fig. 1 without explicit insertions of  $\langle F_\chi \rangle$  and  $\langle \chi \rangle$  in the messenger propagators. In the loop we use mass-eigenstate propagators and insert the diagonalisation matrices at the vertices. Appropriate dependence on  $\langle F_\chi \rangle$  and  $\langle \chi \rangle$  is automatically introduced by the diagonalisation matrices.



**Figure 3:** Two-loop diagrams contributing to the sfermion masses. The long dashed (solid) line is a bosonic (fermionic) messenger. Standard model sfermions are depicted by short dashed lines.

scalar masses. Indeed they are generated by the two-loop diagrams shown in Fig. 3. In [43] the contribution of these diagrams to the sfermion masses was determined to be,

$$m_{\tilde{f}}^2 = \sum_{mess.} \sum_a g_a^4 C_a S_a(mess.) [\text{sum of graphs}], \quad (2.23)$$

where we sum over all gauge groups under which the sfermion is charged,  $g_a$  is the corresponding gauge coupling,  $C_a = (N_a^2 - 1)/(2N_a)$  is the quadratic Casimir and  $S_a(mess.)$  is the Dynkin index of the messenger fields (normalized to 1/2 for fundamentals).

In the following we will only describe the new features specific to the messenger fields of our direct mediation model. The explicit expressions for the loop integrals and the algebraic prefactors resulting from the  $\gamma$ -matrix algebra etc. can be found in the appendix of [43]. To simplify the calculation we also neglect the masses of the MSSM fields relative to the messenger masses.

As in the calculation of the gaugino mass we use the propagators in the diagonal form and insert the diagonalisation matrices directly at the vertices. For the diagrams 3(a) to 3(f) we have closed loops of purely bosonic or purely fermionic mass eigenstates of our messenger fields. It is straightforward to check that in this case the unitary matrices from the diagonalisation drop out. We then simply have to sum over all mass eigenstates the results for these diagrams computed in Ref. [43].

The next diagram 3(g) is slightly more involved. This diagram arises from the D-term interactions. D-terms distinguish between chiral and antichiral fields, in our case  $\rho, Z$  and  $\tilde{\rho}, \tilde{Z}$ , respectively. We have defined our scalar field  $S$  in (2.11) such that all component fields have equal charges. Accordingly, the ordinary gauge vertex is proportional to a unit matrix in the component space (cf. Eq. (2.18)). This vertex is then ‘dressed’ with our diagonalisation matrices when we switch to the  $\hat{S}$  basis, (2.19). This is different for diagram 3(g). Here we have an additional minus-sign between chiral and antichiral fields. In field space this corresponds to a vertex that is proportional to a matrix  $V_D = \text{diag}(1, 1, -1, -1)$ .

We therefore obtain,

$$\text{Fig. 3(g)} = \sum_{i,m} (Q^T V_D Q)_{i,m} J(\hat{m}_{0,m}, \hat{m}_{0,i}) (Q^T V_D Q)_{m,i}, \quad (2.24)$$

where  $J$  is the appropriate two-loop integral for Fig. 3(g) which can be found in [43].

Finally, in 3(h) we have a mixed boson/fermion loop. The subdiagram containing the messengers is similar to the diagram for the gaugino mass. The only difference is the direction of the arrows on the gaugino lines. Indeed the one-loop sub-diagram corresponds to a contribution to the kinetic term rather than a mass term for the gauginos. (The mass term will of course contribute as well but will be suppressed by quark masses.) Using Eq. (2.19) we find,

$$\text{Fig. 3(h)} = \sum_{ik} (|U_{i1}^\dagger Q_{1k} + U_{i2}^\dagger Q_{2k}|^2 + |Q_{k3}^\dagger V_{1i} + Q_{k4}^\dagger V_{2i}|^2) L(\hat{m}_{1/2,i}, \hat{m}_{0,k}), \quad (2.25)$$

where  $L$  is again the appropriate loop integral from [43].

Summing over all diagrams we find the sfermion masses depicted in Fig. 2(b). Comparing to the gaugino masses 2(a) we find the sfermion masses to be significantly bigger. Indeed, the scalar masses roughly follow the naive estimate

$$m_{\tilde{f}}^{2,\text{naive estimate}} \sim \frac{g_A^4}{(16\pi^2)^2} \hat{\mu}^2. \quad (2.26)$$

This demonstrates again the fundamental difference between the generation of gaugino masses and the generation of sfermion masses.

The main results of this section, Eqs. (2.20) and (2.23) give the gaugino and scalar masses generated at the messenger mass scale  $\mu$ . It is useful to factor out the particle-type-dependent overall constants and define the *universal* fermion and scalar mass contributions  $m_{1/2}$  and  $m_0$ , via

$$m_{\lambda_A}(\mu) := \frac{g_A^2}{16\pi^2} m_{1/2} \quad (2.27)$$

$$m_{\tilde{f}}^2(\mu) := \sum_A \frac{g_A^4}{(16\pi^2)^2} C_A S_A m_0^2 \quad (2.28)$$

The main results of this section (2.20) and (2.24) are then expressed in terms of  $m_{1/2}$  and  $m_0$  which we calculate numerically using the VEVs generated by *Vscape*. As an example, in Table 3 we show the values for  $m_{1/2}$  and  $m_0$  obtained for the same parameters as in Table 2. For a more up to date discussion of gaugino and scalar mass values we refer the reader to a more recent paper [15]. In section 4 of that reference we have used more accurate numerical values for stabilised VEVs (with no tree-level constraints imposed) and have also included contributions to  $m_{1/2}$  and  $m_0$  from loops of  $X$  messenger fields.

$\mu$	$m$	$m_{1/2}$	$m_0^2$
10	0.3	$1.03984 \times 10^{-7}$	0.026787
1.1	0.3	0.017843	4.89783
1.01	0.3	0.044771	5.12698
1.003	0.3	0.052320	4.74031

**Table 3:** Gaugino mass and sfermion mass-squared coefficients for various parameter points. All values are in units of  $\hat{\mu}$ .

### 2.3 Renormalisation group running, mass spectrum and electroweak symmetry breaking

In the previous section we calculated the soft SUSY-breaking masses for gauginos and sfermions at the messenger scale  $\mu$ . The Higgs masses  $m_{H_1}^2$  and  $m_{H_2}^2$  are calculated in the same way as the sfermion masses above<sup>7</sup>:

$$m_{H_1}^2(\mu) = m_{H_2}^2(\mu) = \left( \frac{3}{4} \frac{g_2^4}{(16\pi^2)^2} + \frac{3}{20} \frac{g_1^4}{(16\pi^2)^2} \right) m_0^2 \quad (2.29)$$

The other soft SUSY-breaking terms in the MSSM, such as the  $A$ -terms and the  $B$ -term are generated at two-loop level. Indeed the diagrams giving rise to the  $B$ -term require an insertion of the Peccei-Quinn violating parameter  $\mu_{\text{MSSM}}$  and a SUSY breaking gaugino “mass loop”. Thus its magnitude at the messenger scale  $\mu$  is of order [44]

$$B\mu_{\text{MSSM}} \sim \frac{g^2}{16\pi^2} m_\lambda \mu_{\text{MSSM}} \sim \frac{g^4}{(16\pi^2)^2} m_{1/2} \mu_{\text{MSSM}}, \quad (2.30)$$

and is loop suppressed with respect to gaugino masses. For the accuracy required here, it will be sufficient to take  $B = 0$  at the messenger scale.

We now turn to the phenomenology in full, beginning with the SUSY breaking in the visible sector. The next step is to use the renormalisation group running to determine the soft SUSY breaking parameters at the weak scale, solve for electroweak symmetry breaking and find the mass spectrum of the MSSM. We will throughout be using the conventions of Refs. [45,46] (with the obvious replacement  $\mu \rightarrow \mu_{\text{MSSM}}$ ). The pattern of SUSY breaking here is expected to be different from the standard gauge mediation form for two reasons. Firstly our model naturally predicts significantly large values of  $m_0$  relative to  $m_{1/2}$ . Secondly, for reasons explained above, we take  $B = 0$  at the messenger scale. The phenomenology of the  $B = 0$  case has been discussed in refs. [44,48–50]. The main prediction is that high  $\tan \beta$  is required for the electroweak symmetry breaking.

In order to see why, consider the tree level minimization conditions in  $H_2$  and  $H_1$ , which are

$$\mu_{\text{MSSM}}^2 = \frac{m_{H_1}^2 - m_{H_2}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \frac{m_Z^2}{2} \quad (2.31)$$

$$B\mu_{\text{MSSM}} = \frac{\sin(2\beta)}{2} (m_{H_1}^2 + m_{H_2}^2 + 2\mu_{\text{MSSM}}^2). \quad (2.32)$$

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<sup>7</sup>We use the GUT normalisation convention for the  $g_1$  gauge couplings.

Since  $B\mu_{\text{MSSM}}$  is generated only radiatively, the RHS of the second equation has to be suppressed by small  $\sin(2\beta)$  with  $\beta$  approaching  $\pi/2$ . One additional feature of the  $B$ -parameter that complicates the analysis somewhat, is that as noted in Ref. [44] there is an accidental cancellation of renormalization group contributions to its running close to the weak scale. Of course this model becomes more fine-tuned as  $m_0 \gg m_{1/2}$  since we are after all decoupling the supersymmetry in that limit. It is worth understanding what has to be fine-tuned. Since  $\tan\beta \gg 1$  when  $m_0 \gg m_{1/2}$  the first equation tells us that we must have  $\mu_{\text{MSSM}}^2 \approx -m_{H_2}^2$ . In order to have a hope of satisfying the second equation there has to be a cancellation of the terms inside the bracket,  $m_{H_1}^2 + m_{H_2}^2 + 2\mu_{\text{MSSM}}^2 \approx 0$  and therefore  $m_{H_1}^2 \approx m_{H_2}^2$  near the minimization scale. This is consistent with large  $\tan\beta$  where the top and bottom Yukawa couplings become approximately degenerate<sup>8</sup>.

To calculate the spectrum of these models we have modified the *Softsusy2.0* program of Ref. [46]. In its unmodified form this program finds Yukawa couplings consistent with soft SUSY breaking terms (specified at the messenger scale  $Q_{\text{Mess}} = \mu$ ) and electroweak symmetry breaking conditions (imposed at a scale  $Q_{\text{SUSY}}$  to be discussed later). It is usual to take the ratio of Higgs vevs  $\frac{v_u}{v_d} \equiv \tan\beta$  at  $Q_{\text{SUSY}}$  as an input parameter instead of the soft SUSY breaking term  $B\mu_{\text{MSSM}}$  at  $Q_{\text{Mess}}$ . This term, and the SUSY preserving  $\mu_{\text{MSSM}}$  are subsequently determined through the EWSB conditions (2.31),(2.32).

As the models we are considering have  $B\mu_{\text{MSSM}} = 0$  at  $Q_{\text{Mess}}$  to two loops,  $\tan\beta$  is not a free parameter, and must (as noted above) be adjusted in *Softsusy2.0*, so that this boundary condition is met. In detail the iteration procedure works as follows: initially, a high value of  $\tan\beta$  is chosen and all the gauge and Yukawa couplings are evolved to  $Q_{\text{Mess}}$ . The soft parameters are then set, as per the SUSY breaking model, including the condition  $B\mu_{\text{MSSM}} = 0$ . The whole system is then evolved down to  $Q_{\text{SUSY}}$ , where  $\tan\beta$  is adjusted to bring the program closer to a solution of the EWSB condition in Eq.(2.32) (including the 1-loop corrections to the soft masses  $m_{H_1}^2$  and  $m_{H_2}^2$  and the self-energy contributions to the  $\overline{D}\overline{R}$  mass-squared of the axial Higgs,  $m_A^2$ ). We then run back up to  $Q_{\text{Mess}}$  where we reimpose the soft-breaking boundary conditions, and whole the process is repeated until the value of  $\tan\beta$  converges.

The scale  $Q_{\text{SUSY}}$  at which the tree-level minimisation conditions (2.31), (2.32) are imposed is chosen so as to minimise the radiative corrections to the results. It is usually taken to be  $Q_{\text{SUSY}} \equiv x\sqrt{m_{\tilde{t}_1}m_{\tilde{t}_2}}$  where  $x$  (QEWSB in the language of Ref. [46]) is a number of order unity. As we see from Table 4, the lightest Higgs mass (in the model with spontaneously broken  $R$ -symmetry) depends less on scale for lower values of  $Q_{\text{SUSY}}$ , and so in this model we will therefore be using  $Q_{\text{SUSY}} = 0.8 \times \sqrt{m_{\tilde{t}_1}m_{\tilde{t}_2}}$ . Note that only the Higgs masses are sensitive to this choice and the other parameters are largely unaffected.

What the model we are discussing is predicting in most of its parameter space (i.e. generic  $\mu > \hat{\mu}$ ) is clearly split-SUSY like because of the suppression of  $R$ -symmetry violating operators (i.e.  $m_{1/2} \ll m_0$  in Table 2). It provides a first-principles model which can implement split-SUSY [16,17]. (For other realisations of split-SUSY scenarios see e.g. [47].) Our purpose here however is to examine how close models with radiative  $R$ -symmetry breaking can get to the usual gauge mediation scenarios [11]. For

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<sup>8</sup>Using the conventional definition [51], the fine-tuning is then of order  $\mu_{\text{MSSM}}/m_Z$ .



$Q_{\text{SUSY}}$	$\times 0.75$	$\times 0.80$	$\times 0.85$	$\times 0.9$	$\times 0.95$	$\times 0.99$	$\times 1.0$	$\times 1.01$
$h_0$	124.5	124.5	124.2	124.1	123.8	101.5	93.3	78.6

**Table 4:** Checking the scale dependence of the lightest Higgs mass (in GeV).

this reason we want to reduce the  $m_0/m_{1/2}$  ratio as far as possible and to take  $\mu$  approaching  $\hat{\mu}$ , i.e. the last two rows in Table 2. In Table 5 in Section 4, we present a benchmark point (Benchmark Point A) with the full spectrum of the model for  $\mu = 1.003\hat{\mu}$ ,  $m = 0.3\hat{\mu}$ . This point corresponds to a phenomenologically viable region of parameter space near the boundary, that has heavy scalars, and light charginos and neutralinos and exhibits electroweak symmetry breaking. This point is still quite distinct from the usual gauge mediation scenarios, and as we will see in the next section from predictions of gauge mediation models with *explicit*  $R$ -symmetry breaking [12, 13].

### 3. Gauge mediation with explicit $R$ -breaking

Here we consider the gauge mediation models of Refs. [12, 13] which are working models of metastable SUSY breaking with a messenger sector that, as already noted, explicitly breaks the  $R$ -symmetry of the ISS sector. The general philosophy is to appeal to the details of the couplings of the messengers to the electric ISS theory to explain why the explicit  $R$ -symmetry breaking is so weak in the effective theory. The nett result is that one only breaks the  $R$ -symmetry by operators suppressed by powers of  $M_{Pl}$ .

Although the phenomenology is expected to broadly follow that of the gauge mediation paradigm [11], there is a difference. We will argue that, in the present context the Higgs bilinear  $B$  parameter of the MSSM (the SUSY breaking counterpart of  $\mu_{\text{MSSM}} H_u H_d$ ) is naturally zero at the mediation scale. This is because  $R$ -symmetry breaking operators are (by assertion) suppressed by powers of  $M_{Pl}$  and this restricts the possibilities for generating the  $B$  parameter: it is either many orders of magnitude too large or forbidden by symmetries to be zero.

Let us begin by recapping Ref. [12] and considering this issue in detail, before presenting the SUSY breaking phenomenology, and an example benchmark point. The model augments the original ISS model with a pair of messengers “quarks” charged under the SM gauge group denoted  $f$  and  $\tilde{f}$  of mass  $M_f$ . For simplicity we shall assume that they form a fundamental and antifundamental respectively of the parent  $SU(5)$  of the SM. It was proposed that these couple maximally to the electric theory via a piece of the form

$$W_R = \frac{\lambda}{M_{Pl}} (\tilde{Q}Q)(\tilde{f}f) + M_f \tilde{f}f, \quad (3.1)$$

where  $M_{Pl}$  is the scale of new physics at which the operator is generated, hereafter assumed to be the Planck scale. For simplicity we shall for this discussion consider both  $\mu^2$  and  $\lambda$  to be flavour independent couplings. The essential observation of Ref. [12] is that, in the magnetic theory, this appears as an extremely weak violation of  $R$ -symmetry due to the large energy scale at which the

operator is generated

$$W_R = \lambda' \Phi \tilde{f} f + M_f \tilde{f} f \equiv S_{mess} \tilde{f} f \quad (3.2)$$

where we introduced spurion superfield  $S_{mess}$  as in the standard gauge-mediation set-up. By assumption the high energy scale  $M_{Pl}$  is much larger than  $\Lambda$  so that

$$\lambda' = \frac{\lambda \Lambda}{M_{Pl}} \ll 1. \quad (3.3)$$

Since the  $R$ -symmetry is not respected by  $W_R$  the Nelson-Seiberg theorem [19] necessarily leads to the appearance of a new SUSY-preserving vacuum, but as long as  $\lambda'$  is small enough, the transition rate from  $|\text{vac}\rangle_+$  to this new vacuum is suppressed and the original ISS picture is unchanged. Indeed the meson  $\Phi$  field can remain trapped in  $|\text{vac}\rangle_+$  near the origin, with effective messenger  $F$ -term and scalar VEVs of the spurion superfield

$$\begin{aligned} \langle F_{mess} \rangle &\equiv \lambda' \langle F_\Phi \rangle = \lambda' \mu^2 \\ \langle S_{mess} \rangle &\equiv \lambda' \langle \Phi \rangle + M_f \approx M_f \end{aligned} \quad (3.4)$$

As in usual gauge mediation, a gaugino mass is induced at one loop of order

$$m_\lambda \sim \frac{g^2}{16\pi^2} \frac{\langle F_{mess} \rangle}{\langle S_{mess} \rangle} \sim \frac{g^2}{16\pi^2} \frac{\lambda' \mu^2}{M_f} \quad (3.5)$$

and a scalar mass-squared of the same order induced at two loops,

$$m_{\tilde{q}}^2 \sim m_\lambda^2. \quad (3.6)$$

The last equation is a consequence of the fact that  $R$ -symmetry breaking which controls gaugino masses is linked to (i.e. not much smaller than) the SUSY-breaking scale of the Visible Sector.

There is a new global minimum where the rank condition (1.4) is satisfied and the  $\mu^2$ -ISS term is cancelled in the ISS potential,

$$\begin{aligned} \langle \tilde{f} f \rangle &= \mu^2 / \lambda' \\ \langle \Phi \rangle &= M_f / \lambda', \end{aligned} \quad (3.7)$$

however for small enough  $\lambda'$  these minima can be much further from the origin than  $\Lambda$ , beyond which all that one can say is there will be a global minimum of order  $\langle \Phi \rangle \sim \Lambda$ . Such far-flung minima do not change the ISS picture of metastability, and this is why the weakness of  $\lambda'$  is welcome. The resulting bound is  $M_f \gtrsim \lambda' \mu$  [12]. Coupled with the gaugino mass being of order  $m_W$ , we find only very weak bounds:

$$\mu \gtrsim 16\pi^2 m_W. \quad (3.8)$$

There are a number of additional constraints, two of the most important being that  $f$  is non-tachyonic which gives  $M_f^2 > \lambda' \mu^2$ , and that gauge mediation is dominant  $\frac{M_f}{M_{Pl}} \lesssim 10^{-4} \lambda'$ . Additional constraints come from the possibility of additional operators such as  $\delta W = \Phi^2 / M_{Pl}$  which are now allowed in the superpotential, however all of these can be easily satisfied for high values of  $\Lambda$ .

### 3.1 Forbidden operators and $B = 0$

If one considers the MSSM sector as well, then there are other Planck-suppressed  $R$ -symmetry breaking operators that had to be forbidden in Refs. [12, 13]. Normally in gauge mediation one is justified in neglecting gravitationally induced operators altogether, however as we have seen, in these models the leading Planck-suppressed operator plays a pivotal role. Hence it is important to determine what effect other Planck-suppressed operators may have. The most important conclusion of this discussion will be that phenomenological consistency requires  $B \approx 0$  at the mediation scale.

Before considering the operators in question, it is worth recalling the problem with  $B$  in usual gauge mediation, in which supersymmetry breaking is described by a Hidden sector spurion superfield  $S_{mess}$ . The problem arises when one tries to generate the  $\mu_{\text{MSSM}} H_u H_d$  term of the MSSM (for a recent review see Ref. [52]). Consider generating  $\mu_{\text{MSSM}}$  directly in the superpotential. There are two possibilities, either the parameter  $\mu_{\text{MSSM}}$  depends on  $\langle S_{mess} \rangle$  in which case a  $B$ -term is generated, or it does not, in which case  $B = 0$ . Let us suppose that it does, and that the superpotential contains  $W \supset \mu_{\text{MSSM}}(S_{mess}) H_u H_d$ . The  $B$  term is given by

$$B = \frac{\mu'_{\text{MSSM}}}{\mu_{\text{MSSM}}} F_{mess} \sim \frac{F_{mess}}{S_{mess}}, \quad (3.9)$$

where  $\mu'_{\text{MSSM}} = d\mu_{\text{MSSM}}/dS_{mess}$  and the final relation follows from a dimensional analysis. This should be compared with the SUSY breaking contribution to the gaugino masses which appear at one loop,  $m_\lambda \sim \frac{g^2}{16\pi^2} \frac{F_{mess}}{S_{mess}}$ , so that,

$$B \sim \frac{(16\pi^2)}{g^2} m_\lambda. \quad (3.10)$$

Hence one finds that  $B\mu_{\text{MSSM}}$  is two orders of magnitude too large. More generally because the  $\mu_{\text{MSSM}}$  and  $B\mu_{\text{MSSM}}$  terms are both forbidden by a Peccei-Quinn symmetry, they tend to be generated at the same order, whereas  $B\mu_{\text{MSSM}}$  should have an additional loop suppression (in order to be comparable to the scalar mass-squareds). One can then assume that  $\mu_{\text{MSSM}}$  is independent of  $S_{mess}$  in which case  $B = 0$ , or try to find a more sophisticated dynamical reason that the  $B$  term receives loop suppression factors.

Now let us turn to the models of Ref. [12, 13]. Here the situation is rather more pronounced for the very same reason that the  $R$ -symmetry breaking is under control, namely that the spurion is related to a meson of the electric theory. The  $\mu_{\text{MSSM}}$  term will be a function of

$$\frac{Q\tilde{Q}}{M_{Pl}} = \frac{\Lambda\Phi}{M_{Pl}}, \quad (3.11)$$

and will be dominated by the leading terms. The leading operators involving  $H_2 H_1$  we can consider are

$$\begin{aligned} W &\supset \mu_0 H_2 H_1 + \frac{\lambda_2}{M_{Pl}} H_2 H_1 \tilde{f} f + \frac{\lambda_3}{M_{Pl}} H_2 H_1 \tilde{Q} Q, \\ K &\supset \lambda_4 \frac{(Q\tilde{Q})^\dagger H_2 H_1}{M_{Pl}^2} + h.c.. \end{aligned} \quad (3.12)$$

where  $\lambda_{2,3,4} \sim 1$ . We will for generality allow the  $\mu_0$  term which is consistent with  $R$ -symmetry in the renormalizable theory; this represents supersymmetric contributions to the  $\mu_{\text{MSSM}}$ -term that do not involve the ISS sector. (It would of course be inconsistent to allow further SUSY breaking in the non-ISS sector.) The remaining  $R$ -violating operators we will take to be Planck suppressed as prescribed in refs. [12, 13].

Unfortunately it is clear that the Kahler potential term cannot (as it could in Refs. [53, 54]) be responsible for the  $\mu_{\text{MSSM}}$ -term. Its contribution is of order

$$\mu_{\text{MSSM}} \sim \frac{\Lambda}{M_{Pl}^2} \mu^2 \quad (3.13)$$

but we require  $\mu^2 \ll M_{Pl} m_W$  for gauge-mediation to be dominant, which would imply  $\mu_{\text{MSSM}} \ll \frac{\Lambda}{M_{Pl}} m_W$ . Similar consideration apply to operators in the Kahler potential with factors of  $D^2(\Phi^\dagger \Phi)$  as in [55].

Turning instead to the leading superpotential terms, and assuming the messengers remain VEV-less, one has

$$\begin{aligned} \mu_{\text{MSSM}} &= \mu_0 + \lambda_3 \frac{\Lambda}{M_{Pl}} \langle \Phi \rangle \sim \mu_0 + \lambda_3 16\pi^2 \frac{\Lambda^3}{M_{Pl}^2} \\ B\mu_{\text{MSSM}} &= \lambda_3 \frac{\Lambda \mu^2}{M_{Pl}} \\ m_{Higgs}^2 &\sim \frac{g^4}{(16\pi^2)^2} \frac{\Lambda^2}{M_{Pl}^2 M_f^2} \mu^4 \\ m_\lambda &\sim \frac{g^2}{16\pi^2} \frac{\Lambda}{M_{Pl}} \frac{\mu^2}{M_f}, \end{aligned} \quad (3.14)$$

where we used the fact that, as shown in Ref. [12], the  $\Phi$  field is expected to get only a small VEV due to the presence of  $R$ -symmetry breaking operators, which was estimated to be

$$\langle \Phi \rangle \sim 16\pi^2 \frac{\Lambda^2}{M_{Pl}}. \quad (3.15)$$

The above gives

$$B\mu_{\text{MSSM}} \sim \frac{16\pi^2}{g^2} m_\lambda M_f. \quad (3.16)$$

Typically  $M_f$  has to be orders of magnitude above  $m_W$ , so the situation is considerably worse than in usual gauge mediation unless a symmetry forbids the  $\lambda_3$  coupling. A global  $R$ -symmetry would not be respected by gravitationally suppressed operators, however it *is* possible that particular operators can be suppressed. If  $\mu_{\text{MSSM}}$  for example is charged under an additional gauge symmetry then one might expect

$$\lambda_2 \sim \lambda_3 \sim \frac{\mu_{\text{MSSM}}}{M_{Pl}}, \quad (3.17)$$

in which case the effect of these operators is utterly negligible and we effectively have

$$\begin{aligned} \mu_{\text{MSSM}} &\approx \mu_0 \\ B &\approx 0. \end{aligned} \quad (3.18)$$

Note the importance of the interpretation of the effective ISS theory as a magnetic dual in this discussion. For example one could also have considered the effective operator

$$W_{R/MSSM} = \frac{\lambda_4}{M_{Pl}} H_2 H_1 \text{Tr}(\tilde{\varphi} \cdot \varphi). \quad (3.19)$$

This would have given  $\mu_{MSSM} \sim \frac{\mu^2}{M_{Pl}}$  similar to the Giudice-Masiero mechanism, above. However because the magnetic quarks  $\varphi$  and  $\tilde{\varphi}$  are composite objects, the coupling  $\lambda_4$  will be suppressed by many powers of  $\Lambda/M_{Pl}$  so this contribution to  $\mu_{MSSM}$  would always be negligible.

Finally, we have investigated the pattern of SUSY breaking in the model with explicit  $R$ -breaking [12, 13], discussed above. As expected, it conforms to the standard gauge mediation form, with a requirement that  $B = 0$  at the mediation scale. In Table 5 in Section 4, we present a benchmark point (Benchmark Point B) with the full spectrum of the model.

## 4. Conclusions

It can be argued that in generic models of low scale supersymmetry breaking (where gravity effects can be neglected) metastability is inevitable.

In this paper we compared SUSY-breaking patterns generated in two distinct and complementary scenarios of gauge-mediated supersymmetry breaking. Both scenarios employ an explicit formulation of the Hidden Sector in terms of an ISS-like gauge theory with a long-lived metastable vacuum. This, in both cases, provides a simple and calculable model to implement metastable DSB.

The difference between the two approaches lies in the mechanism of  $R$ -symmetry breaking. The first one, described in Section 2, employs spontaneous  $R$ -symmetry breaking induced by radiative corrections. It is based on the direct gauge mediation model introduced in [14]. We find that  $R$ -symmetry violating soft terms (such as gaugino masses) tend to be suppressed with respect to  $R$ -symmetry preserving ones, leading to a scenario with large scalar masses. These models effectively interpolate between split SUSY models and standard gauge mediation.

The second approach, outlined in Section 3 is based on gauge mediation models of Refs. [12, 13] with a messenger sector that explicitly breaks the  $R$ -symmetry of the ISS sector by operators suppressed by powers of  $M_{Pl}$ . We argue that these models lead to phenomenology broadly similar to standard gauge mediation, but with an additional constraint that  $B = 0$  at the mediation scale.

Determining the complete spectrum of superpartner masses at benchmark points (see Table 5) we find that apart from high values of  $\tan \beta$  (arising from the condition that  $B \approx 0$  at the messenger scale in both models) the phenomenology of these models is quite different. For the model with explicit  $R$ -symmetry breaking (Benchmark Point B) we find that it follows closely the usual gauge mediation scenario where gauginos and sfermions have roughly equal masses. In contrast the model

	Model A	Model B
$Q_{\text{Mess}}$	$8.32 \times 10^5$	$1 \times 10^7$
$\tan \beta$	58.7	38.9
$\text{sgn} \mu_{\text{MSSM}}$	+	+
$\mu_{\text{MSSM}}(Q_{\text{SUSY}})$	2891	939
$\tilde{e}_L, \tilde{\mu}_L$	4165	747.9
$\tilde{e}_R, \tilde{\mu}_R$	2133	399.8
$\tilde{\tau}_L$	1818	319.4
$\tilde{\tau}_R$	4093	737.5
$\tilde{u}_1, \tilde{c}_1$	11757	1963
$\tilde{u}_2, \tilde{c}_2$	11205	1867
$\tilde{t}_1$	10345	1593
$\tilde{t}_2$	11061	1825
$\tilde{d}_1, \tilde{s}_1$	11784	1973
$\tilde{d}_2, \tilde{s}_2$	11144	1851
$\tilde{b}_1$	10298	1754
$\tilde{b}_2$	11060	1822
$\chi_1^0$	60.8	270.3
$\chi_2^0$	125.0	524.8
$\chi_3^0$	2906	949.0
$\chi_4^0$	2929	950.3
$\chi_1^\pm$	100.7	526.5
$\chi_2^\pm$	2894	945.6
$h_0$	124.8	137.6
$A_0, H_0$	184.5	975.1
$H^\pm$	207.4	978.6
$\tilde{g}$	414.2	1500
$\tilde{\nu}_{1,2}$	4175	740.2
$\tilde{\nu}_3$	4095	724.4

**Table 5:** Sparticle spectra for SUSY breaking models with spontaneously broken (Model A) and explicitly broken (Model B)  $R$ -symmetry. All masses are in GeV.

with spontaneous  $R$ -symmetry breaking typically has sfermions that are considerably heavier than the gauginos – resembling a scenario of split SUSY. Benchmark Point A represents such a model at a region in parameter space where the ‘split aspects’ of supersymmetry are minimal.<sup>9</sup> At the same time it is quite distinct from the usual gauge mediation scenarios, having relatively heavy scalars and light charginos and neutralinos.

We conclude that details of the dynamics of the Hidden Sector – the nature of  $R$ -symmetry and

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<sup>9</sup>A more up to date discussion of such models can be found in [15].

SUSY-breaking – leave a clear imprint on the phenomenology of the MSSM. Although the general gauge mediation scenario incorporates both of these scenarios, there is enough flexibility in GMSB to distinguish them. It would be interesting to broaden this study to other models with either spontaneous or explicit  $R$ -symmetry breaking, to see if the general pattern outlined here persists.

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## A. The $R$ -symmetry of the baryon-deformed ISS model

It is known that the  $R$ -symmetry of the ISS SQCD manifests itself only as an approximate symmetry of the magnetic formulation which is broken explicitly in the electric theory by the mass terms of electric quarks  $m_Q$ . Here we want to quantify this statement and show that the  $R$ -symmetry breaking in the microscopic theory is controlled by small parameter,  $m_Q/\Lambda = \mu^2/\Lambda^2 \ll 1$ . As such the intrinsic  $R$ -breaking effects and deformations can be neglected. This justifies the approach we follow in section 2 where the  $R$ -symmetry of the magnetic theory is used to constrain the allowed deformations. Consequently, the  $R$ -symmetry-preserving baryon deformation in Eq. (2.1) gives a generic superpotential.

We first consider the massless undeformed SQCD theory, its global symmetry is  $SU(N_f)_L \times SU(N_f)_R \times U(1)_B \times U(1)_A \times \overline{U(1)}_R$ . Following the well-established conventions [56] the  $\overline{U(1)}_R$  symmetry is taken to be anomaly-free, and the axial symmetry  $U(1)_A$  is anomalous. (The  $U(1)_R$  symmetry of our section 2 will be constructed below as an anomalous linear combination of the  $\overline{U(1)}_R$ ,  $U(1)_A$  and  $U(1)_B$  above.) Table 6 lists the charges of matter fields of the electric and the magnetic formulations. The scale  $\Lambda$  is charged only under the  $U(1)_A$  which identifies it as the anomalous  $U(1)$ . In the usual fashion, the  $U(1)_A$ -charge of  $\Lambda$  in Table 6 is determined from the nonperturbative superpotential, cf. Eq. (1.3),

$$W_{\text{dyn}} = (N_f - N_c) \left( \frac{\det_{N_f} \tilde{Q} Q}{\Lambda^{3N_c - N_f}} \right)^{\frac{1}{N_f - N_c}} \quad (\text{A.1})$$

Table 6 also shows that the superpotential  $W$  is charged only under the  $\overline{U(1)}_R$  which identifies it as the  $R$ -symmetry (such that  $\int d^2\theta W$  is neutral).

Finally, the charges of magnetic quarks  $\varphi, \tilde{\varphi}$  are derived from the matching between electric and magnetic baryons,  $B_E/\Lambda^{N_c} = B_M/\Lambda^{N_f - N_c}$ ,  $\tilde{B}_E/\Lambda^{N_c} = \tilde{B}_M/\Lambda^{N_f - N_c}$  which implies (schematically)

$$\left( \frac{\varphi}{\Lambda} \right)^{N_f - N_c} = \left( \frac{Q}{\Lambda} \right)^{N_c}, \quad \left( \frac{\tilde{\varphi}}{\Lambda} \right)^{N_f - N_c} = \left( \frac{\tilde{Q}}{\Lambda} \right)^{N_c}. \quad (\text{A.2})$$

	$SU(N_f)_L$	$SU(N_f)_R$	$U(1)_B$	$U(1)_A$	$\overline{U(1)}_R$
$Q$	$\square$	$\mathbf{1}$	1	1	$\frac{N_f - N_c}{N_f}$
$\tilde{Q}$	$\mathbf{1}$	$\bar{\square}$	-1	1	$\frac{N_f - N_c}{N_f}$
$\Lambda$	$\mathbf{1}$	$\mathbf{1}$	0	$\frac{2N_f}{3N_c - N_f}$	0
$W$	$\mathbf{1}$	$\mathbf{1}$	0	0	2
$\varphi$	$\bar{\square}$	1	$\frac{N_c}{N_f - N_c}$	$\frac{2N_f - 3N_c}{3N_c - N_f}$	$\frac{N_c}{N_f}$
$\tilde{\varphi}$	1	$\square$	$-\frac{N_c}{N_f - N_c}$	$\frac{2N_f - 3N_c}{3N_c - N_f}$	$\frac{N_c}{N_f}$
$\Phi = \frac{Q\tilde{Q}}{\Lambda}$	$\square$	$\bar{\square}$	0	$2 - \frac{2N_f}{3N_c - N_f}$	$2\frac{N_f - N_c}{N_f}$

**Table 6:** Charges under the global  $SU(N_f)_L \times SU(N_f)_R \times U(1)_B \times U(1)_A \times \overline{U(1)}_R$

	$U(1)_B$	$U(1)_A$	$\overline{U(1)}_R$
$Q$	1	1	$\frac{2}{7}$
$\tilde{Q}$	-1	1	$\frac{2}{7}$
$\Lambda$	0	$\frac{7}{4}$	0
$W$	0	0	2
$\varphi$	$\frac{5}{2}$	$-\frac{1}{8}$	$\frac{5}{7}$
$\tilde{\varphi}$	$-\frac{5}{2}$	$-\frac{1}{8}$	$\frac{5}{7}$
$\Phi$	0	$\frac{1}{4}$	$\frac{4}{7}$

**Table 7:** Charges under  $U(1)_B \times U(1)_A \times \overline{U(1)}_R$  for  $N_c = 5$  and  $N_f = 7$

The charges of  $\Phi$  are read off its definition,  $\Phi = \frac{Q\tilde{Q}}{\Lambda}$ . As a consistency test on these charges, one can easily verify that the magnetic superpotential  $W = \varphi\Phi\tilde{\varphi}$  is automatically neutral under  $U(1)_A$ ,  $U(1)_B$  and has the required charge 2 under the  $R$ -symmetry.

We now introduce mass terms  $m_Q\tilde{Q}Q$  in the superpotential of the electric theory. We want to continue describing the symmetry structure in terms of the parameters of the IR magnetic theory. For this purpose we use for quark masses  $m_Q = \frac{\mu^2}{\Lambda}$ . This mass-deformation breaks the flavour group  $SU(N_f)_L \times SU(N_f)_R$  to the diagonal  $SU(N_f)$  (if, for example, all quark masses were the same). It also breaks  $U(1)_A \times \overline{U(1)}_R$ , to a linear combination  $U(1)$  subgroup. If in addition, we introduce the baryon deformation, as in section 2, it breaks the third  $U(1)_B$  factor. In total, the combined effect of the two deformations breaks  $U(1)_B \times U(1)_A \times \overline{U(1)}_R$  to a single  $U(1)_R$ . This is the  $R$ -symmetry of section 2 and it is anomalous since  $\Lambda$  is charged under it.<sup>10</sup>

To explicitly construct this surviving  $U(1)_R$  for the model of section 2, we set  $N_c = 5$  and  $N_f = 7$  and list the three  $U(1)$  charges in Table 7. It is now clear that the  $U(1)_R$  symmetry of section 2 is

<sup>10</sup>Note that the two deformations are associated with orthogonal  $U(1)$ 's and are therefore independent.



	$U(1)_R$
$\varphi$	1
$\tilde{\varphi}$	-1
$\Phi$	2
$\Lambda$	10
$\mu$	0
$W$	2
$Q$	$6 + \frac{2}{5}$
$\tilde{Q}$	$6 - \frac{2}{5}$
$m_Q = \frac{\mu^2}{\Lambda}$	-10

**Table 8:** Charges under  $U(1)_R$  for  $N_c = 5$  and  $N_f = 7$

the linear combination of the three  $U(1)$ 's with the charge

$$R = \overline{R} + \frac{40}{7} A + \frac{2}{5} B \quad (\text{A.3})$$

This is the unique unbroken linear combination surviving the mass- plus the baryon-deformation,  $-\mu^2\Phi + m\varphi^2$ , of the magnetic theory with the charges listed in Table 8. In the magnetic Seiberg-dual formulation, the  $U(1)_R$  symmetry is manifest. It is the symmetry of the perturbative superpotential (2.1) which is only broken anomalously.

In the electric formulation the  $U(1)_R$  symmetry is broken by the mass terms  $m_Q \tilde{Q}Q$  on the account of the explicit  $\Lambda$ -dependence of the masses  $m_Q = \frac{\mu^2}{\Lambda}$ . It is also broken by the baryon deformation (again in the electric theory language)  $\frac{1}{M_{Pl}^2} Q^5$  because the magnetic baryon deformation parameter  $m$  in (2.3) explicitly depends on  $\Lambda$ . Thus the apparent  $U(1)_R$  symmetry of the IR theory is only approximate, and is lifted in the UV theory. However, the  $R$ -symmetry is broken in a controlled way, by the parameter of the order of  $m_Q/\Lambda$ . To verify this note that in the limit  $m_Q \rightarrow 0$ , the electric quark masses disappear while the baryon deformation  $\frac{1}{M_{Pl}^2} Q^5$  is invariant under the  $R$ -symmetry  $U(1)_{R'}$ :

$$R' = \overline{R} + \frac{5}{7} A - \frac{3}{5} B \quad (\text{A.4})$$

This is a different from (A.3) linear combination, but in the massless limit we are considering it is a perfectly valid classically conserved  $R$ -symmetry which protects the baryon deformation in the electric theory and forbids e.g. anti-baryon deformations  $\frac{1}{M_{Pl}^2} \tilde{Q}^5$ . Thus in the massless limit there is always an  $R$ -symmetry which protects baryon deformations either in the electric or in the magnetic formulation. When quark masses are non-vanishing, this  $R$ -symmetry is broken by  $m_Q/\Lambda$ . Indeed, if one formally sends  $\Lambda \rightarrow \infty$  holding  $\mu$  and  $m$  fixed, the dynamical non-perturbative superpotential disappears and the exact  $U(1)_R$  is recovered.

In general, anomalous global symmetries do not match in the magnetic and the electric descriptions. The  $U(1)_R$  is an approximate symmetry and in principle one should allow generic  $U(1)_{R'}$ -violating deformations. For example, one can add an antibaryon  $\tilde{B}$  deformation to the superpotential

(2.1). However, these deformations are suppressed relative to the  $U(1)_R$ -preserving ones by the small parameter,  $m_Q/\Lambda = \mu^2/\Lambda^2 \ll 1$ , and therefore can be neglected.

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